



# *Article* **Active-Learning Approaches for Landslide Mapping Using Support Vector Machines**

**Zhihao Wang [\\*](https://orcid.org/0000-0001-6342-5784) and Alexander Brenning**

Department of Geography, Friedrich Schiller University Jena, Loebdergraben 32, 07743 Jena, Germany; alexander.brenning@uni-jena.de

**\*** Correspondence: zhihao.wang@uni-jena.de

**Abstract:** Ex post landslide mapping for emergency response and ex ante landslide susceptibility modelling for hazard mitigation are two important application scenarios that require the development of accurate, yet cost-effective spatial landslide models. However, the manual labelling of instances for training machine learning models is time-consuming given the data requirements of flexible data-driven algorithms and the small percentage of area covered by landslides. Active learning aims to reduce labelling costs by selecting more informative instances. In this study, two common active-learning strategies, uncertainty sampling and query by committee, are combined with the support vector machine (SVM), a state-of-the-art machine-learning technique, in a landslide mapping case study in order to assess their possible benefits compared to simple random sampling of training locations. By selecting more "informative" instances, the SVMs with active learning based on uncertainty sampling outperformed both random sampling and query-by-committee strategies when considering mean AUROC (area under the receiver operating characteristic curve) as performance measure. Uncertainty sampling also produced more stable performances with a smaller AUROC standard deviation across repetitions. In conclusion, under limited data conditions, uncertainty sampling reduces the amount of expert time needed by selecting more informative instances for SVM training. We therefore recommend incorporating active learning with uncertainty sampling into interactive landslide modelling workflows, especially in emergency response settings, but also in landslide susceptibility modelling.

**Keywords:** active learning; landslide modelling; support vector machine; machine learning

## **1. Introduction**

Despite significant progress in landslide hazard assessment and mitigation, these hazards still present a major challenge for policymakers to reduce monetary losses and casualties. The occurrence probability of landslides, which broadly include a large variety of downslope movement processes on hillslopes under the effects of gravity [\[1\]](#page-12-0), varies greatly in space and time as a result of complex patterns of predisposing factors and temporal variation in triggering factors. Considering the ongoing global trends of urbanization, deforestation, and climate change, landslide science faces the growing challenge of having to update landslide hazard assessments and provide rapid post-disaster information in the event of regional triggering events such as rainstorms and earthquakes [\[2](#page-12-1)[–4\]](#page-12-2). For example, an earthquake in Tomakomai, Japan triggered about 10,000 landslides causing 36 deaths [\[3\]](#page-12-3), and in 2018, landslides triggered by seasonal heavy precipitation caused approximately 105 deaths and USD 212 million in losses in China [\[5\]](#page-12-4). In Italy, as in many other regions worldwide, landslides are mostly triggered by intense or prolonged rainfall [\[6\]](#page-13-0). These hazards often cause long-term economic loss, population displacement, and negative effects on the natural environment.

Landslide mapping refers to the manual or automated detection and delineation of actual landslides that are appreciable in remote-sensing imagery or based on their topographic footprint [\[7](#page-13-1)[–9\]](#page-13-2). Additionally, the growing availability of light detection and



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ranging (LiDAR) derived high-resolution digital terrain models (HRDTM) allows us to detect landslides where passive optical sensors are limited (e.g., within the forest) [\[10,](#page-13-3)[11\]](#page-13-4). This classification task is related to landslide susceptibility mapping, which focuses on estimating the probability of future landslide occurrences based on predisposing factors: usually topographic, geological, and land use/land cover conditions. Evidently, factors that control susceptibility can also provide valuable information for landslide mapping [\[12\]](#page-13-5), which also requires post-event remote-sensing data (e.g., optical or LiDAR). Conversely, landslide inventories created by means of landslide mapping are a necessary input for landslide susceptibility mapping using supervised classification models. Together, landslide mapping and susceptibility modelling play a critical role in providing information that is necessary for decision making in emergency situations and for reducing risk in the development of spatial planning strategies.

Machine-learning techniques are increasingly being adopted in landslide modelling, as they have the potential to better adapt to complex nonlinear Earth surface processes and their interactions with land use than parametric statistical techniques such as logistic regression. Examples for black-box machine-learning models include the SVM, artificial neural networks, and random forests, whereas the generalized additive model (GAM) as an intermediate-complexity model is popular due to its nonlinear but more interpretable structure [\[13–](#page-13-6)[16\]](#page-13-7). However, these data-driven supervised learning algorithms need a large number (e.g., thousands) of observations of landslide presence/absence, which are usually derived from manually digitized landslide inventories. Creating landslide inventories and more generally the manual labelling or annotation of these instances is a very timeconsuming task, which increases the cost of landslide modelling studies and leads to delays in post-disaster situation awareness.

Active learning (AL) is a framework that promises to reduce this burden by selecting "informative" instances for the user to label  $[17,18]$  $[17,18]$ . In each of these queries to the user, an additional small batch of unlabelled instances (e.g., grid cells) is selected based on an informativeness measure and then presented to an "oracle" (i.e., a human annotator) for labelling. Active learning aims to achieve better accuracies using as few labelled instances as possible, thereby minimizing the cost of obtaining labelled data. Active learning has increasingly been adopted in remote-sensing classification [\[19](#page-13-10)[–21\]](#page-13-11) but has rarely been adopted in the context of landslide mapping [\[22\]](#page-13-12).

The SVM has become increasingly popular in the context of landslide modelling along with other nonlinear techniques such as the generalized additive model [\[15,](#page-13-13)[23,](#page-13-14)[24\]](#page-13-15). Compared to the less flexible GAM, the SVM is capable of modelling nonlinear interactions among predictors while avoiding overfitting through regularization. Therefore, active learning based on the SVM for predicting landslides was adopted in this paper.

Hence, the main objective of this study is to assess the potential of different activelearning strategies for landslide mapping based on limited amounts of labelled data. We consider two popular active-learning query strategies in combination with the SVM in a case study from the Andes of southern Ecuador [\[25\]](#page-13-16).

#### **2. Materials and Methods**

In this study, we use active-learning strategies [\[26\]](#page-13-17) to sample "interesting" (i.e., informative) locations for training SVM models for landslide detection, and we compare this approach to a simple random sampling strategy (Figure [1\)](#page-2-0). In active learning, a small training data set is initially retrieved to obtain a preliminary SVM fit. This model's classifications then allow us to identify relevant additional instances that have the greatest potential to improve the model fit. These instances are then labelled, and the SVM is retrained with the additional training data. This step is repeated to investigate changes in model performance with increasing instance size. Hyperparameters are tuned in each individual step, and model performances are estimated in identical test sets to ensure comparability. Details of this procedure are explained in the following sections, and Settles (2010) [\[26\]](#page-13-17) provides a detailed overview of active-learning strategies.

<span id="page-2-0"></span>

**Figure 1.** Overview of the workflow of active learning for landslide detection based on the SVM.

### *2.1. Active-Learning and Traditional Learning Strategies Used*

Active learning is a subfield of machine learning that is also referred to as query learning or optimal experimental design in the statistical literature. It is a very broad field encompassing many different approaches [\[26](#page-13-17)[–30\]](#page-13-18). In general, the purpose of active learning is to require as few labelled instances as possible while achieving a level of high accuracy. After starting with a small initial training set, small batches of additional "informative" instances are presented to an expert for labelling.

There are three different settings of active learning, namely membership query synthesis, stream-based selective sampling, and pool-based sampling [\[26,](#page-13-17)[27\]](#page-13-19). For our study area, we have a large collection of unlabelled data. Due to uncertainty in the random generation process of instances using membership query synthesis [\[31\]](#page-13-20) and the high cost of labelling selected instances one by one using stream-based selective sampling, pool-based sampling was adopted in this study. Pool-based sampling can be further divided into two main categories: uncertainty sampling and query by committee [\[19\]](#page-13-10).

We denote the unlabelled data set as x and the classes of the unlabelled data set as y. P $_{\theta}$  is the posterior probability as estimated by the current model  $\theta$  in a given activelearning step.

#### 2.1.1. Uncertainty Sampling

Uncertainty sampling chooses the instances that are predicted with the lowest confidence, i.e., that are associated with the greatest uncertainty in the current model [\[32\]](#page-13-21). It may be the most common and simplest active-learning approach. We briefly present three popular uncertainty-sampling strategies, but we choose only margin sampling due to the mathematical equivalence of these approaches in two-class situations.

## (1) Least Confidence

The least-confidence strategy for a sequence of models queries the instances for which the current model has the least confidence as the predicted classes are equally likely [\[33\]](#page-13-22). Therefore, the most "informative" instances are selected by

$$
\hat{y} = \operatorname{argmax}_{y} P_{\theta}(y|x),\tag{1}
$$

$$
x_{LC}^{*} = \operatorname{argmax}_{x} (1 - P_{\theta}(\hat{y}|x)), \tag{2}
$$

where  $\hat{y}$  is the most likely label, i.e., the class label with the highest posterior probability under the current model  $\theta$ .  $x_{\text{LC}}^*$  represents the instance that the current model  $\theta$  is most likely to mislabel.

(2) Margin Sampling (MS)

Margin sampling (MS) was proposed to additionally take advantage of information regarding the posterior probabilities of all of the labels, not only the most likely one [\[34\]](#page-13-23). Here, instances with the smallest margin between the posterior of the first and the second most likely labels are selected. Since these are more ambiguous, the model has difficulty in differentiating between the two most likely class labels. Hence, knowing the true label would help the classifier to discriminate them more effectively. The instances are selected using

$$
x_{\text{MS}}^* = \operatorname{argmin}_{x} (P_{\theta}(\hat{y}_1|x) - P_{\theta}(\hat{y}_2|x)), \tag{3}
$$

where  $\hat{y_1}$  and  $\hat{y_2}$  are the first and the second most likely labels, respectively.

#### (3) Entropy measure

One of the more general pool-based sampling strategies is based on the entropy measure [\[35\]](#page-14-0). This strategy uses entropy, which is an information-theoretic measure of uncertainty of a random variable. It aims at using information from all of the remaining classes to detect the most informative instances. Intuitively, the entropy measure strategy should perform better than the least-confidence and MS strategies, especially for very large label sets. Instances are selected using

$$
E(y, x) = -\sum_{i=1}^{k} P_{\theta}(y_i|x) \log P_{\theta}(y_i|x), \qquad (4)
$$

$$
x_{EP}^* = \text{argmax}_x E(y, x), \tag{5}
$$

where  $E(y, x)$  is the entropy value of class y for instance *x*. Instances with the highest entropy value, which imply more uncertainty in the distribution, are selected as  $x_{EP}^*$ .

Each of these uncertainty sampling strategies have their own application scenarios. In binary classification, however, all three are equivalent in selecting instances with the posterior class probabilities closest to 0.5 [\[26\]](#page-13-17). We implemented uncertainty sampling using the equation given for margin sampling, and we therefore refer to it as margin sampling in the rest of the paper.

## 2.1.2. Query by Committee

Query by committee (QBC) is another more theoretically motivated active learning algorithm that selects informative unlabelled instances based on different models (a committee) trained on the current labelled training set [\[26](#page-13-17)[,36\]](#page-14-1). Based on the posterior probabilities predicted by the different committee members, the unlabelled instances with the maximum disagreement are selected. Two important measures of disagreement among the models are the Kullback–Leibler (KL) divergence [\[37,](#page-14-2)[38\]](#page-14-3) and vote entropy [\[39\]](#page-14-4). Because KL divergence applies several independent justifications and calculates the average difference between the label distributions of any committee, it is considered the better approach to selecting informative instances [\[30\]](#page-13-18). Hence, KL divergence was adopted in this study. Let  $C = \{\theta(1), \ldots, \theta(C)\}\$  denotes the set of models forming the committee. Then

$$
P_C(y_i|x) = \frac{1}{|C|} \sum_{c=1}^{C} P_{\theta(c)}(y_i|x),
$$
 (6)

corresponds to the committee's average posterior probability of class label  $y_i$ , and

$$
D(P_{\theta(c)}||P_C) = \sum_{i} P_{\theta(c)}(y_i|x) \log(P_{\theta(c)}(y_i|x)/P_C(y_i|x)),
$$
\n(7)

denotes the KL divergence, which we try to maximize on average over all committee members:

$$
x_{KL}^* = \text{argmax}_{x \in C} \frac{1}{C} \sum_{c=1}^{C} D(P_{\theta(c)} || P_C),
$$
\n(8)

This strategy focuses on the instances  $x_{KL}^*$  with the larger average difference with respect to the label distributions of any one committee.

Various strategies can be applied to creating a committee, such as bootstrap resampling of the training data [\[40](#page-14-5)[,41\]](#page-14-6). We decided to set up a committee of SVM classifiers trained using different hyperparameter values since the behaviour of the SVM strongly varies with its cost and bandwidth parameters, C and  $\gamma$  [\[42\]](#page-14-7). In each active-learning round, we randomly sampled 250 pairs of hyperparameter values (log<sub>2</sub> C between  $-12$  and +15 and log<sub>2</sub> γ between −12 and +6). The best-performing 25 hyperparameter settings were then selected to form a committee for that round.

## 2.1.3. Random Sampling as a Baseline

In addition to the active-learning strategies described above, simple random sampling (RS) was used for comparison. It randomly selects instances from the unlabelled data with equal probability and does not try to assess the utility of the data for landslide mapping.

### *2.2. Landslide Classification Model*

In this study we used a support vector machine (SVM) model, which is a flexible supervised machine-learning technique [\[43\]](#page-14-8). It has previously shown competitive performances in landslide modelling [\[12](#page-13-5)[,15](#page-13-13)[,44](#page-14-9)[,45\]](#page-14-10). This technique is particularly appealing in active learning because its flexibility can be tuned extremely well, allowing it to transition from a strongly penalized simple model to a more complex one as the sample size grows larger. The SVM can be applied in both one-class and two-class cases. Yao, et.al. (2008) compared one-class and two-class SVM on landslide analysis and concluded that two-class SVM could have better prediction efficiency than one-class SVM [\[46\]](#page-14-11). Therefore, in this study, we applied two-class SVM as the active-learning classifier.

Because the flexibility of the SVM is controlled by its hyperparameters  $\gamma$  (bandwidth) and C (cost), a k-fold cross-validation was used in each active-learning iteration to optimize them [\[47\]](#page-14-12). In this cross-validation, the training set is split into k equally sized partitions, one of which is retained for testing the model, and the remaining  $k - 1$  partitions are used as training data. This process is repeated k times, and every partition is used once as the validation data. Performance estimates are averaged over the k partitions to obtain a crossvalidation estimate of the performance measure. We used  $k = 10$ , which is a commonly used setting. Given the spatial nature of our data, we used k-means clustering of the sample coordinates to generate spatial cross-validation partitions [\[48\]](#page-14-13). The choice of the SVM kernel function is less critical; therefore, the radial basis function kernel was adopted.

The area under the receiver operating characteristic (ROC) curve [\[49](#page-14-14)[,50\]](#page-14-15) (AUROC) [\[51\]](#page-14-16) was used as a measure of predictive performance. Its range is between 0.5 (no predictive skill) and 1 (perfect separation).

#### *2.3. Repetition and Performance Estimation*

The workflow described above was repeated 150 times in order to eliminate the influence of random variability on our results. In active learning as well as random sampling, we draw an additional batch 25 points in each iteration or epoch after an initial random sample of 210 points in the first step. This initial data contains 10 landslide points and 200 non-landslide points, roughly representing the spatial landslide density within the study area. With the chosen batch size, on average, one additional landslide point will be drawn from the study area even in random sampling, given the 4% landslide density. We performed 50 iterations in order to observe the convergence of results for large instance sizes, although such large sample sizes (1460 labelled instances) are not of practical relevance.

The entire study area (87,223 non-landslide and 2569 landslide gird cells) as the target area for landslide mapping was used for analysing and comparing AUROC performances obtained by SVMs with active- (MS, QBC) and passive-learning strategies (RS). We extracted 55,887 non-landslide and 1663 landslide grid cells from the overall data set to serve as a pool of candidate grid cells from which we sampled the training data set.

In order to gain insight into the importance of predictors at different active-learning stages, we further calculated the permutation-based variable importance as a simple overall measure of predictive importance [\[52\]](#page-14-17). This was applied in a spatial cross-validation framework, i.e., by making predictions on spatially disjoint cross-validation test sets [\[53\]](#page-14-18). Accumulated local effects (ALE) [\[54\]](#page-14-19) plots were further generated to visualize the shape of the relationships between important predictor variables and SVM landslide classifications.

All statistical analyses were conducted using the open-source statistical software R (version 3.6.3) [\[55\]](#page-14-20) and its contributed packages "sperrorest" for spatial cross-validation [\[56\]](#page-14-21), "e1071" for SVM modelling [\[57\]](#page-14-22), "ROCR" for AUROC estimation [\[58\]](#page-14-23), and "iml" for model interpretation [\[59\]](#page-14-24). The R package "RSAGA" [\[60\]](#page-14-25) and the open-source GIS SAGA [\[61\]](#page-14-26) were used for geodata processing.

#### *2.4. Study Area and Data*

The study area of our case study is located in the Andes of Southern Ecuador in the Reserva Biológica San Francisco (RBSF). The RBSF is located between the provincial capitals of Loja and Zamora (3°58'30" S, 79°4'25" W) [\[62\]](#page-14-27). The slopes are steep (1st quartile of slope angle: 28.8°, median: 36.5°) and covered with evergreen lower and upper mountain rainforest [\[63\]](#page-15-0). The annual precipitation in the study area ranges from 2000 mm in the lower parts to more than 6000 mm between 2900 and 3100 m a.s.l. with nearly daily rainfall [\[64\]](#page-15-1). This area is characterized by a high frequency of landslide occurrences, which underlines the potential utility of active-learning techniques for generating event-based landslide inventories on demand with as little labelling as possible. In this study area, landslides are important ecosystem disturbances that trigger local vegetation successions and thus contribute to habitat complexity in this unique hotspot of plant biodiversity [\[65](#page-15-2)[,66\]](#page-15-3). Landslide processes were previously studied in more detail with a focus on geomorphic process rates and the possible effects of human land use [\[25](#page-13-16)[,67\]](#page-15-4). In this case study, we focus on the "natural" part of the RBSF study area of Muenchow et al. (2012). The dataset includes 178 landslides with a mean landslide size of 793  $m^2$ . We refer the reader to Muenchow et al. (2012) for further geomorphological detail and an analysis of landslide susceptibility [\[25\]](#page-13-16).

We used a high-resolution orthorectified aerial photograph of the study area as a direct optical indicator of vegetation disturbance by landslides. The image was acquired in 2001 and has a 0.3 m  $\times$  0.3 m spatial resolution (data source: E. Jordan and L. Ungerechts, Düsseldorf; DFG Research Unit FOR 816). Small cloudy patches and other errors were masked out manually (Figure [2\)](#page-6-0). Landslides were mapped in this imagery by J. Muenchow (Erlangen), who analyzed the landslide distribution and characteristics in this study in more detail as part of a regional-scale comparison [\[25\]](#page-13-16).

Vegetation indices (VIs) play an important role in mapping landslides and other forest disturbances [\[68,](#page-15-5)[69\]](#page-15-6). Although the near-infrared part of the spectrum is particularly useful for identifying photosynthetically active, healthy plants, the imagery available for this case study is limited to the visible part of the spectrum, while having the benefit of offering the resolution required to detect the narrow, elongated landslides of this study area. Considering the spectral characteristics of the available orthophoto, we used the green chromatic coordinate (GCC) vegetation index [\[70\]](#page-15-7), which has been shown to compare favourably to other indices in the visible part of the spectrum in distinguishing the forest from the soil [\[71\]](#page-15-8). The GCC is generally effective in suppressing the effects of changes in scene illumination [\[72\]](#page-15-9), which is important in our mountainous study area. GCC is defined as

$$
GCC = G/(R + B + G),
$$
\n(9)

where R, G, and B represent the red, green, and blue bands of the ortho-photo. The red (RCC) and blue (BCC) chromatic coordinates are calculated in the same way. Because RCC

<span id="page-6-0"></span>

and BCC are strongly correlated (correlation coefficient: 0.95), we used GCC as a vegetation index as well as RCC.

Figure 2. The study area: the Reserva Biológica San Francisco (RBSF), (a) hillshade with 10 m  $\times$  10 m resolution in 1997, and (**b**) the orthophoto with 0.3 m  $\times$  0.3 m resolution in early 2001.

A digital elevation model (DEM) of the RBSF at a 10 m  $\times$  10 m resolution produced by E. Jordan and L. Ungerechts (Düsseldorf) was generated from stereo aerial photographs<br>contrario diameters in the spectrum is particularly in the spectrum is particular to the spectrum is a spectrum attributes from the DEM, as they are commonly included in landslide distribution models the study is limited to the visible part of the spectrum, while having the spectrum, while having the spectrum of  $\sigma$  as preparatory factors: local slope angle (slope), plan and profile curvature (plancurv and profcurv), and the slope angle (cslope) and logarithm of the size of the upslope contributing area (log.carea) [15]. These terrain attributes are intended to act as proxies for destabilizing forces (slope, cslope), water availability (log.carea, concave curvatures), and exposure to wind (convex curvatures) as well as general variability in the characteristics of soil and vegetation [\[25\]](#page-13-16). Our expectation is that these terrain attributes will further improve  $\alpha$  in scene in scene in scene in our mountainous study area. The in our mountainous study area. The intervals study area. from the year 1997. Following Muenchow et al. (2012) [\[25\]](#page-13-16), we derived the following terrain landslide classification.

Exercise Sensing variables. Predictors that presented outliers were winsorized at the 1st and records. Overall, our feature set consisted of five terrain attributes and the GCC and RCC as 99th percentile.

## **3. Results**

# where R, G, and B represent the red, green, and blue bands of the ortho-photo. The red *3.1. Model Performance*

Overall, active learning using margin sampling outperformed query by committee and random sampling after only four epochs, i.e., starting with a learning instance size of 310 grid cells (Figure [3\)](#page-7-0). The SVM with MS increased continuously from this point, going from 0.80 in epoch 3 with only 285 grid cells to 0.83 after epoch 8, i.e., with label information for >410 grid cells. Mean AUROCs obtained with RS and QBC were very similar; they both reached  $\sim$ 0.79 for only large sample sizes. The similar performances of QBC as an active-learning strategy and RS for passive learning suggest that the instances labelled in QBC-based active learning were no more informative than the ones retrieved with simple  $\ddot{\text{Q}}$ random sampling. Nevertheless, SVM performances with QBC were less variable than<br>these correlated with BC upse completed (later terms) [15]. The intended terms are interested to act as in the set as in the set as in the set as in the set of a contributes are in the set of act as in the set of act as in the set of act as in the those completed with RS.

<span id="page-7-0"></span>

sampling methods in the target area. Figure 3. Performance versus epochs: mean AUROCs of SVMs across all 150 repetitions for different sampling includes in the target area.

Similarly, the random variability of AUROC performances over the 150 repetitions<br>revealed much less variable results for MS-based active learning than for OBC and RS were at least twofold across all epochs, which indicates that informative instance data not<br>only improves the performance but also reduces the probability of obtaining poor results only improves the performance but also reduces the probability of obtaining poor results<br>due to rendom verichility revealed much less variable results for MS-based active learning than for QBC and RS, which show similar results (Figure 4). Differences in variability between MS and QBC/RS due to random variability.

<span id="page-7-1"></span>

Figure 4. **Standard deviation of AUROC estimates and AUROC estimates and AUROC estimates and SUS Figure 4.** Standard deviation of AUROC estimates across all 150 repetitions for different sampling methods in the target area.

higher cost values when combined with larger γ values (Figure [5\)](#page-8-0). Considering the importance of the cost and gamma hyperparameters for the flexibility  $\frac{1}{2}$  consider the comparation were increasingly concentrated around the  $2^0$  to  $2^5$  region and the optimal  $\gamma$  to around 2<sup>−5</sup>, although the optimal region extended diagonally towards higher acative line and the optimal region extended diagonally towards  $\sigma$  in margin sampling sampling. As the sampling sample size increased, the optimal cost increased, the optimal cost of the SVM, we examined the variability in optimal hyperparameters for different activelearning epochs in margin sampling. As the sample size increased, the optimal cost

<span id="page-8-0"></span>

**Figure 5.** Optimal hyperparameters for the SVM with margin sampling in epochs 0, 5, 10, and 20 **Figure 5.** Optimal hyperparameters for the SVM with margin sampling in epochs 0, 5, 10, and 20 for for all 150 repetitions. all 150 repetitions.

## *3.2. Model Interpretation*

*3.2. Model Interpretation*  A permutation-based variable importance assessment for the SVM with margin sampling revealed that the most important predictors were GCC and RCC, which was followed by a logarithm of the catchment area and catchment slope (Figure [6\)](#page-8-1). Thus, predictors that mance of models for landslide mapping consistently across all epochs. Note that there are mance of models for landslide mapping consistently across all epochs. Note that there are moderate to strong correlations between the slope variables as well as between the upslope contributin[g](#page-9-0) area and the two curvature variables (Table 1). are commonly used in landslide susceptibility modelling helped to improve the perfor-

<span id="page-8-1"></span>

Figure 6. Variable importance plot for SVM using margin sampling in each epoch.<br> **Figure 6.** Variable importance plot for SVM using margin sampling in each epoch.

ALE plots for the 20th epoch of the 1st repetition display the averaged relationships between predictors and responses (Figure [7\)](#page-9-1). Broadly speaking and as expected, landslides are primarily characterized by low vegetation vigour as represented by a low vegetation index, and to a smaller extent, by a steep upslope area. They are also rarely found in the valley bottoms, where the upslope contributing area is large, or directly on ridges or hilltops, where the upslope contributing area would be small. Ridges and hilltops often show reduced vegetation canopy due to factors other than landslides, such as windthrow, and the inclusion of the upslope contributing area therefore reduces confounding with these patterns, resulting in a geomorphologically more plausible classification.

<span id="page-9-0"></span>



 $\frac{100}{\text{Local slope angle}}$  (slope), plan and profile curvature (plancurv and profcurv), the slope angle (cslope) and logarithm of the size of the upslope contributing area (log.carea), and green chromatic coordinate (GCC) and red chromatic coordinate (RCC).

## **Predictors**

<span id="page-9-1"></span>

logarithm of the size of the upslope contributing area, log.carea) for the SVM with margin sampling in repetition 1, epoch 20. **Figure 7.** ALE plots of the most important predictors (green chromatic coordinate, GCC; red chromatic coordinate, RCC;

matic coordinate, RCC; logarithm of the size of the upslope contributing area, log.carea) for the Landslide maps predicted by SVM with margin sampling clearly depict many of the the relatively stable model performances and variable importance reported above. Despite the visual similarities between epochs 5 and 10, it should be remembered that quantitative  $\frac{1}{2}$ performances in terms of the mean and standard deviation of AUROC did substantially<br>improve from epoch 5 to epoch 10, as hyperparameter tuning started to stabilize as well the relation stable model performance reports and variable input of the stable input of the stable in port of th landslide-affected areas even after only five epochs (Figure [8\)](#page-10-0). There is little change in the spatial pattern of mapped landslides after more than five epochs, which is consistent with performances in terms of the mean and standard deviation of AUROC did substantially

<span id="page-10-0"></span>

Figure 8. Landslide classification maps of SVM with margin sampling in epochs 0, 5, 10, and 20. Predicted probabilities are classified into four classes (very high, high, moderate, and low) using the top 4th, 10th, and 50th percentile as boundaries. class boundaries.

#### **4. Discussion**  $<sub>Discu</sub>$  to be misclassified by the model and labelling the model and labelling the model and labelling therefore has  $\sim$ </sub>

## **4.1. Potential of SVM with AL**

Overall, our results confirm the potential of AL for remote-sensing applications and for landslide mapping in particular [\[19,](#page-13-10)[22\]](#page-13-12), and demonstrate the suitability of uncertainty<br>sampling strategies. AI, retrieves the data that it believes is more likely to be misclassisampling strategies. AL retrieves the data that it believes is more likely to be misclassified [26]. For the learning process of SVM, it builds a margin to classify the instances based its features. If a new candidate point's distance from the margin is too small, this instance<br>is more likely to be misclessified by the model and lebelling these instances therefore hes is more likely to be misclassified by the model and labelling these instances therefore has the greatest potential to improve model performance.

Landslide data is always imbalanced, which poses a particular challenge in classifica-<br> tion modelling that can be addressed using uncertainty sampling. In this study, landslides covered only 4% of the study area, and consequently, random sampling is very poor at collecting information on positives. In contrast, AL strategies can reduce the impact of imbalance by retrieving more "useful" instances, including more positives (Table [2](#page-11-0) and Figure [9\)](#page-11-1). This is especially true for MS.

<span id="page-11-0"></span>**Table 2.** Number of landslide and non-landslide instances in the training set after 50 epochs using different sampling strategies. strategies.



<span id="page-11-1"></span>

Figure 9. *Figure 9.*   $\mathbf{F}$  is the training set in the training set in each epoch using SVM with different set in each epoch using SVM with different set in the training  $\mathbf{F}$  and  $\mathbf{F}$  and  $\mathbf{F}$  are the tra **Figure 9.** Number of landslide instances in the training set in each epoch using SVM with different sampling strategies.

## sampling strategies. *4.2. Limitations of SVM with AL*

*4.2. Limitations of SVM with AL*  on posterior probability, they are sensitive to SVM hyperparameters. If hyperparameters cannot be renably estimated, as is the case in the initial epochs with small sample sizes,<br>model performance can be highly variable and sometimes poor (Figures [3](#page-7-0) and [4\)](#page-7-1). When this occurs, AL query strategies may be close to random sampling, or they may even oversample irrelevant regions in the featured space [\[73,](#page-15-10)[74\]](#page-15-11). The QBC strategy may be particularly<br>consitive to this much law sings SVM a with 25 different hyperparameter settings were used to form a committee. In general, it can be difficult to strike the right balance between diversity A possible limitation of AL in the context of SVM classification is the interaction between the hyperparameters and the query strategy. Specifically, since AL queries depend cannot be reliably estimated, as is the case in the initial epochs with small sample sizes, sensitive to this problem since SVMs with 25 different hyperparameter settings were used to

and goodness-of-fit of committee members, and the use of the top hyperparameter settings may not achieve an optimal committee. Although other strategies could be used, it was beyond the scope of this work to experiment with these additional design options. Xu et al. (2020) used three different pre-trained SVMs as committee members to conduct classifications and concluded that pre-trained SVMs made QBC more robust in iterative training [\[42\]](#page-14-7). Stumpf formed QBC committees using 500 fully grown trees from a random forest (RF) and concluded they can achieve good results [\[22\]](#page-13-12), but no comparison with other, model-independent QBC approaches or with other query strategies was made. Considering these limitations and the positive results achieved with uncertainty sampling strategies, we suggest that the latter offers several advantages ranging from a simpler, model-agnostic implementation to fewer design decisions and reduced computational cost.

#### **5. Conclusions**

In this study, active-learning strategies for training landslide detection models outperformed models trained using randomly sampled data. The mean AUROCs of the SVM with margin sampling as an active-learning strategy was 0.80 with only 285 instances and 0.83 with 410 instances. In contrast, SVMs with query-by-committee and random sampling achieved AUROCs around 0.79 but only for large sample sizes. Meanwhile, the SVM with margin sampling was more robust than the other strategies. Therefore, uncertainty sampling is particularly promising as it achieved the best performance, was best able to handle imbalanced data, and is straightforward to implement regardless of the machine-learning model being used.

Labelling a large number of instances using human experts is a time-consuming process that cannot be executed in sufficient detail under time constraints, e.g., in emergency situations. Additionally, human experts cannot recognize which additional instances would be the most "useful" for predicting the response to, or in our case for identifying, landslides. Active-learning methods are therefore a promising strategy as part of an interactive landslide detection workflow, especially in an emergency response setting.

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